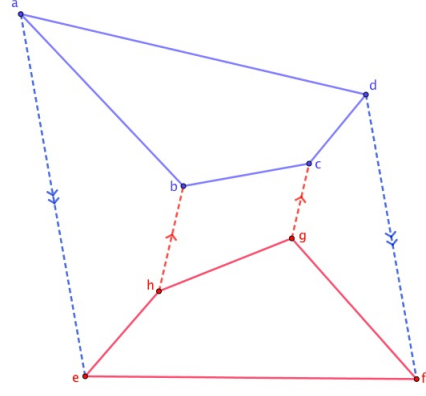


Known results:

- (1) The area of the triangle abc is $\frac{i}{4}(a\bar{b} + b\bar{c} + c\bar{a} - \bar{a}b - \bar{b}c - \bar{c}a)$
 (2) Consider the triangle whose one vertex is 0 , and the remaining two are x and y .
 If h is the orthocenter of triangle then $h = \frac{(\bar{x}y + x\bar{y})(x-y)}{xy - \bar{x}}$



Solution:

Assume that a is the origin ($a = 0$) in the complex plane and ac is the real axis ($\bar{c} = c$). According to (2) we have:

$$\triangle ABC : e = \frac{(b+\bar{b})(b-c)}{b-\bar{b}}, \bar{e} = -\frac{(b+\bar{b})(\bar{b}-c)}{b-\bar{b}}, \triangle CDA : g = \frac{(\bar{d}+d)(c-d)}{\bar{d}-d}; \bar{g} = -\frac{(\bar{d}+d)(c-\bar{d})}{\bar{d}-d}, \triangle DAB : h = \frac{(b\bar{d}+\bar{b}d)(b-d)}{b\bar{d}-\bar{b}d}; \bar{h} = -\frac{(b\bar{d}+\bar{b}d)(\bar{b}-\bar{d})}{b\bar{d}-\bar{b}d}$$

$$\left. \begin{aligned} DF \perp BC &\Leftrightarrow \frac{d-f}{\bar{d}-\bar{f}} = -\frac{b-c}{\bar{b}-\bar{c}} \\ CF \perp BD &\Leftrightarrow \frac{c-f}{\bar{c}-\bar{f}} = -\frac{b-d}{\bar{b}-\bar{d}} \end{aligned} \right\} \Rightarrow \begin{cases} f = \frac{(d+\bar{d}-b-\bar{b})c^2 - (d^2+d\bar{d}-b^2-b\bar{b})c + b\bar{d}\bar{d} + d^2\bar{b} - b\bar{d}\bar{b} - b^2\bar{d}}{(b+\bar{d}-d-\bar{b})c + d\bar{b} - b\bar{d}} \\ \bar{f} = -\frac{(d+\bar{d}-b-\bar{b})c^2 - (d^2+d\bar{d}-\bar{b}^2-b\bar{b})c + \bar{b}d\bar{d} + b\bar{d}^2 - b\bar{d}\bar{b} - d\bar{b}^2}{(b+\bar{d}-d-\bar{b})c + d\bar{b} - b\bar{d}} \end{cases}$$

$$[ABCD] = [ABC] + [CDA] = \frac{i}{4}(b - \bar{b} + \bar{d} - d)c$$

After some algebra we get:

$$[EFGH] = [EFH] + [HFG] = \frac{i}{4}(e\bar{f} + h\bar{e} - f\bar{e} - e\bar{h} + f\bar{g} + g\bar{h} - g\bar{f} - h\bar{g}) = \dots = \frac{i}{4}(b - \bar{b} + \bar{d} - d)c$$